

$$B_{\hat{z}(r < R)} = at\hat{z}$$

$$\Phi_B = at\pi R^2$$

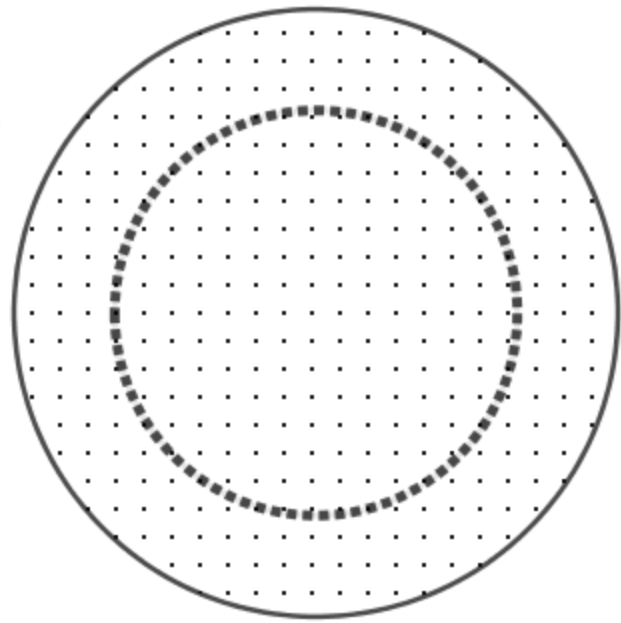
$$\epsilon = \dot{\Phi}_B = a\pi R^2$$

$$\epsilon = \int_0^{2\pi r} \vec{E} \cdot d\vec{l} = 2\pi r \cdot \vec{E}$$

$$\frac{a\pi R^2}{2\pi} \frac{1}{r} = \vec{E}_\theta$$

$$\vec{\nabla} \times \vec{E} = -\frac{\partial B}{\partial t}$$

$$\begin{aligned}\vec{\nabla} \times \vec{E} = & \left( \frac{1}{r} \frac{\partial E_{\hat{z}}}{\partial \theta} - \frac{\partial E_{\hat{\theta}}}{\partial z} \right) \hat{r} \\ & \left( \frac{\partial E_{\hat{r}}}{\partial z} - \frac{\partial E_{\hat{z}}}{\partial r} \right) \hat{\theta} \\ & \frac{1}{r} \left[ \frac{\partial (r E_{\hat{\theta}})}{\partial r} - \frac{\partial E_{\hat{r}}}{\partial \theta} \right] \hat{z}\end{aligned}$$



$$B_{\hat{z}(r<\infty)} = at\hat{z}$$

$$\Phi_B = at\pi r^2$$

$$\epsilon = \dot{\Phi}_B = a\pi r^2$$

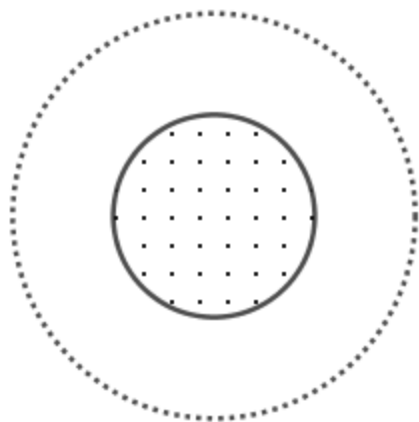
$$\epsilon = \int_0^{2\pi r} \vec{E} \cdot d\vec{l} = 2\pi r \cdot \vec{E}$$

$$\vec{\nabla} \times \vec{E} = -\frac{dB}{dt}$$

$$\vec{\nabla} \times \vec{E} = \left( \frac{1}{r} \frac{\partial E_{\hat{z}}}{\partial \theta} - \frac{\partial E_{\hat{\theta}}}{\partial z} \right) \hat{r} + \left( \frac{\partial E_{\hat{r}}}{\partial z} - \frac{\partial E_{\hat{z}}}{\partial r} \right) \hat{\theta} + \frac{1}{r} \left[ \frac{\partial(rE_{\hat{\theta}})}{\partial r} - \frac{\partial E_{\hat{r}}}{\partial \theta} \right] \hat{z}$$

$$\frac{a\pi}{2\pi} r = \vec{E}_{\hat{\theta}}$$

$$I_{(r < R)(t)} = at\hat{z} \Rightarrow B_{(t)} = \frac{at}{r}\hat{\theta}$$



$$\vec{\nabla} \times \vec{E} = -\frac{\partial B}{\partial t}$$

$$\begin{aligned} \vec{\nabla} \times \vec{E} &= \left( \frac{1}{r} \frac{\partial E_z}{\partial \theta} - \frac{\partial E_{\hat{\theta}}}{\partial z} \right) \hat{r} \\ &\quad \left( \frac{\partial E_{\hat{r}}}{\partial z} - \frac{\partial E_z}{\partial r} \right) \hat{\theta} \\ &\quad \frac{1}{r} \left[ \frac{\partial(rE_{\hat{\theta}})}{\partial r} - \frac{\partial E_{\hat{r}}}{\partial \theta} \right] \hat{z} \end{aligned}$$

$$-\frac{\partial B}{\partial t} = -\frac{a}{r}\hat{\theta} = \vec{\nabla} \times \vec{E} = -\frac{\partial E_z}{\partial r}\hat{\theta}$$

$$\frac{a}{r} = \frac{\partial E_z}{\partial r}$$

$$\vec{E}_z = a \int \frac{1}{r}$$

$$\vec{E}_z = a \cdot \ln(r)$$